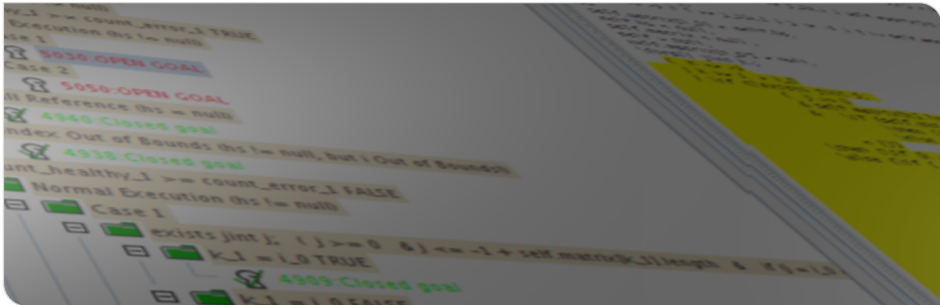


Integrating Source Code, Specification, and Proof State into a Single View in Key

Wolfram Pfeifer | August 12, 2022



Deductive verifier for (sequential) Java



Deductive verifier for (sequential) Java Java Modeling Language (JML)



Deductive verifier for (sequential) Java
Java Modeling Language (JML)
Modular specification/verification



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification

Dynamic Logic (JavaDL), sequent calculus



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

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Dynamic Logic (JavaDL), sequent calculus

Automatic and interactive application of rules



Deductive verifier for (sequential) Java

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Automatic and interactive application of rules

Optional translation to SMT-LIB



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification

Dynamic Logic (JavaDL), sequent calculus

Automatic and interactive application of rules

Optional translation to SMT-LIB

Symbolic Execution



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification

Dynamic Logic (JavaDL), sequent calculus

Automatic and interactive application of rules

Optional translation to SMT-LIB

Symbolic Execution

Dynamic Frames



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification

Dynamic Logic (JavaDL), sequent calculus

Automatic and interactive application of rules

Optional translation to SMT-LIB

Symbolic Execution

Dynamic Frames

Counterexample generation

Information flow proofs

Testcase generation

...



Run CVC5, Princess, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

with model src@4:49:20 PM

SumAndMaxSumAndMax:sumAndMax

Proof Search Strategy

Proof

Proof

Proof Tree

0:OPEN GOAL

Sequent

Current Goal

wellFormed(heap)

```

 $\wedge$   $\neg$ self = null
 $\wedge$  self.<created> = TRUE
 $\wedge$  SumAndMax::exactInstance(self) = TRUE
 $\wedge$  (a = null  $\vee$  a.<created> = TRUE)
 $\wedge$  measuredByEmpty
 $\wedge$  (  $\forall$  int i; (0  $\leq$  i  $\wedge$  i < a.length  $\wedge$  inInt(i)  $\rightarrow$  0  $\leq$  a[i])
 $\wedge$  (self.<inv>  $\wedge$  a = null))
- {heapAtPre:=heap || _a:=a}
  \{
    exc=null;try {
      self.sumAndMax(_a)@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc=e;
    }
  }\> {  $\forall$  int i;
    ( 0  $\leq$  i  $\wedge$  i < a.length  $\wedge$  inInt(i)
       $\rightarrow$  a[i]  $\leq$  self.max)
 $\wedge$  ( ( a.length > 0
      -  $\exists$  int i;
        ( 0  $\leq$  i
           $\wedge$  i < a.length
           $\wedge$  inInt(i)
           $\wedge$  self.max = a[i]))
 $\wedge$  ( self.sum
      = (int)(bsum(int i;)(0, a.length, a[i]))
 $\wedge$  ( self.sum
       $\leq$  javaMulInt(a.length, self.max)
       $\wedge$  self.<inv>))
 $\wedge$  exc = null
 $\wedge$   $\forall$  Field f;
 $\forall$  java.lang.Object o;
  ( (o, f)  $\in$  {(self, SumAndMax::$sum)
    U {(self, SumAndMax::$max)}}
 $\vee$   $\neg$ o = null
 $\wedge$   $\neg$ o.<created>@heapAtPre = TRUE
 $\vee$  o.f = o.f@heapAtPre)

```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @           ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23     @ && (k == 0 ==> max == 0)
24     @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25     @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @
28     @ assignable sum, max;
29     @ decreases a.length - k;
30     @*/
31     while(k < a.length) {
32       if(max < a[k]) {
33         max = a[k];
34       }
35       sum += a[k];
36       k++;
37     }
38   }
39 }
40

```

Show Postcondition/Assignable

File View Proof Options Origin Tracking

About

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with model src@4:49:20 PM

SumAndMaxSumAndMax:sumAndMax

Proof Search Strategy Goals

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Proof Tree

0: OPEN GOAL

Sequent

Current Goal

```

wellFormed(heap)
 $\wedge \neg \text{self} = \text{null}$ 
 $\wedge \text{self}.\langle \text{created} \rangle = \text{TRUE}$ 
 $\wedge \text{SumAndMax}::\text{exactInstance}(\text{self}) = \text{TRUE}$ 
 $\wedge (\text{a} = \text{null} \vee \text{a}.\langle \text{created} \rangle = \text{TRUE})$ 
 $\wedge \text{measuredByEmpty}$ 
 $\wedge (\forall \text{int } i; (0 \leq i \wedge i < \text{a}.\text{length} \wedge \text{inInt}(i) \rightarrow 0 \leq \text{a}[i])$ 
 $\wedge (\text{self}.\langle \text{inv} \rangle \wedge \neg \text{a} = \text{null}))$ 
- {heapAtPre:=heap ||  $\_a := \text{a}$ }
  \{
    exc=null; try {
      self.sumAndMax( $\_a$ )@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc=e;
    }
  } \> {  $\forall \text{int } i;$ 
    (  $0 \leq i \wedge i < \text{a}.\text{length} \wedge \text{inInt}(i)$ 
       $\rightarrow \text{a}[i] \leq \text{self}.\text{max}$ )
     $\wedge (\text{a}.\text{length} > 0$ 
       $\rightarrow \exists \text{int } i;$ 
        (  $0 \leq i$ 
           $\wedge i < \text{a}.\text{length}$ 
           $\wedge \text{inInt}(i)$ 
           $\wedge \text{self}.\text{max} = \text{a}[i])$ )
     $\wedge (\text{self}.\text{sum}$ 
       $= (\text{int})(\text{bsum}(\text{int } i;)(0, \text{a}.\text{length}, \text{a}[i]))$ 
       $\wedge (\text{self}.\text{sum}$ 
         $\leq \text{javaMulInt}(\text{a}.\text{length}, \text{self}.\text{max})$ 
         $\wedge \text{self}.\langle \text{inv} \rangle$ )
     $\wedge \text{exc} = \text{null}$ 
     $\wedge \forall \text{Field } f;$ 
       $\forall \text{java.lang.Object } o;$ 
        ( (o, f)  $\in$  {(self, SumAndMax::$sum)
          U {(self, SumAndMax::$max)})
           $\wedge \neg o = \text{null}$ 
           $\wedge \neg o.\langle \text{created} \rangle @ \text{heapAtPre} = \text{TRUE}$ 
           $\wedge \forall o.f = o.f @ \text{heapAtPre}$ )
  }

```

precondition ϕ

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallforall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallforall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @           ==> (\existsexists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   */
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ && (\forallforall int i; 0 <= i && i < k; a[i] <= max)
23     @ && (k == 0 ==> max == 0)
24     @ && (k > 0 ==> (\existsexists int i; 0 <= i && i < k; max == a[i]))
25     @ && sum == (\sum sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @
28     @ assignable a.length, max;
29     @ decreases a.length - k;
30     */
31   while(k < a.length) {
32     if(max < a[k]) {
33       max = a[k];
34     }
35     sum += a[k];
36     k++;
37   }
38 }
39 }
40

```

Show Postcondition/Assignable

Proof has been pruned: one open goal remains.

Show log

File View Proof Options Origin Tracking

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SumAndMax@SumAndMax:sumAndMax

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0: OPEN GOAL

Sequent

Current Goal

```

wellFormed(heap)
 $\wedge \neg self = null$ 
 $\wedge self.<created> = TRUE$ 
 $\wedge SumAndMax::exactInstance(self) = TRUE$ 
 $\wedge (a = null \vee a.<created> = TRUE)$ 
 $\wedge measuredByEmpty$ 
 $\wedge (\forall int\ i; (0 \leq i \wedge i < a.length \wedge inInt(i) \rightarrow 0 \leq a[i])$ 
 $\wedge (self.<inv> \wedge \neg a = null))$ 
- {heapAtPre:=heap || _a:=a}
  \{
    exc=null; try {
      self.sumAndMax(_a)@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc=e;
    }
  }
\}> (  $\forall int\ i;$ 
  (  $0 \leq i \wedge i < a.length \wedge inInt(i)$ 
    -  $a[i] \leq self.max$ )
   $\wedge$  ( (  $a.length > 0$ 
    -  $\exists int\ i;$ 
      (  $0 \leq i$ 
         $\wedge i < a.length$ 
         $\wedge inInt(i)$ 
         $\wedge self.max = a[i]$ )
      )
    )
  )
 $\wedge$  ( self.sum
  = (int)(bsum(int i;)(0, a.length, a[i]))
  )
 $\wedge$  ( self.sum
   $\leq$  javaMulInt(a.length, self.max)
  )
 $\wedge$  self.<inv>))
 $\wedge$  exc = null
 $\wedge \forall$  Field f;
   $\forall$  java.lang.Object o;
  ( (o, f)  $\in$  {(self, SumAndMax::$sum)
    U {(self, SumAndMax::$max)}}
  )
  )
 $\wedge \neg o = null$ 
 $\wedge \neg o.<created>$ @heapAtPre = TRUE
 $\wedge o.f = o.f$ @heapAtPre)

```

precondition ϕ program p

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @           ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   */
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23     @ && (k == 0 ==> max == 0)
24     @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25     @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @
28     @ assignable a.length - k;
29     @ decreases a.length - k;
30     */
31   while(k < a.length) {
32     if(max < a[k]) {
33       max = a[k];
34     }
35     sum += a[k];
36     k++;
37   }
38 }
39 }
40

```

Show Postcondition/Assignable

Proof has been pruned: one open goal remains.

Show log

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SumAndMax@SumAndMax:sumAndMax

Proof Search Strategy

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0: OPEN GOAL

Sequent

Current Goal

```

wellFormed(heap)
 $\wedge \neg self = null$ 
 $\wedge self.<created> = TRUE$ 
 $\wedge SumAndMax::exactInstance(self) = TRUE$ 
 $\wedge (a = null \vee a.<created> = TRUE)$ 
 $\wedge measuredByEmpty$ 
 $\wedge ( \forall int\ i; (0 \leq i \wedge i < a.length \wedge inInt(i) \rightarrow 0 \leq a[i])$ 
 $\wedge (self.<inv> \wedge \neg a = null))$ 
- {heapAtPre:=heap || _a:=a}

```

precondition ϕ

```

<<
exc=null;try {
  self.sumAndMax(_a)@SumAndMax;
} catch (java.lang.Throwable e) {
  exc=e;
}

```

program p

```

}> {  $\forall int\ i;$ 
  (  $0 \leq i \wedge i < a.length \wedge inInt(i)$ 
 $\rightarrow a[i] \leq self.max$ )
 $\wedge ( ( a.length > 0$ 
 $\rightarrow \exists int\ i;$ 
  (  $0 \leq i$ 
 $\wedge i < a.length$ 
 $\wedge inInt(i)$ 
 $\wedge self.max = a[i]))$ 
 $\wedge ( self.sum$ 
 $= (int)(bsum(int\ i;)(0, a.length, a[i]))$ 
 $\wedge ( self.sum$ 
 $\leq javaMulInt(a.length, self.max)$ 
 $\wedge self.<inv>))$ 
 $\wedge exc = null$ 
 $\wedge \forall Field\ f;$ 
 $\forall java.lang.Object\ o;$ 
  ( (o, f)  $\in \{(self, SumAndMax::\$sum)$ 
 $\cup \{(self, SumAndMax::\$max)\}$ 
 $\vee \neg o = null$ 
 $\wedge \neg o.<created>@heapAtPre = TRUE$ 
 $\vee o.f = o.f@heapAtPre)$ 

```

postcondition ψ

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @           ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   */
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
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20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
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24     @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25     @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @
28     @ assignable a.length, max;
29     @ decreases a.length - k;
30     */
31   while(k < a.length) {
32     if(max < a[k]) {
33       max = a[k];
34     }
35     sum += a[k];
36     k++;
37   }
38 }
39 }
40

```

Show Postcondition/Assignable

Show log

Proof has been pruned: one open goal remains.

Run CVC5, Princess, Z3

Layouts: Default Load Layout Save Layout Reset Layout

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with model src@4:49:20 PM

SumAndMaxSumAndMax:sumAndMax

Proof Search Strategy Goals

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Proof Tree

0:OPEN GOAL

Sequent

Current Goal

wellFormed(heap) $\wedge \neg \text{self} = \text{null}$ $\wedge \text{self}.\langle \text{created} \rangle = \text{TRUE}$ $\wedge \text{SumAndMax}::\text{exactInstance}(\text{self}) = \text{TRUE}$ $\wedge (\text{a} = \text{null} \vee \text{a}.\langle \text{created} \rangle = \text{TRUE})$ $\wedge \text{measuredByEmpty}$ $\wedge (\forall \text{int } i; (0 \leq i \wedge i < \text{a}.\text{length} \wedge \text{inInt}(i) \rightarrow 0 \leq \text{a}[i]))$ $\wedge (\text{self}.\langle \text{inv} \rangle \wedge \neg \text{a} = \text{null})$ $\neg \{\text{heapAtPre} := \text{heap} \mid _ \text{a} := \text{a}\}$

\{

\{

exc=null;try {

self.sumAndMax(_a)@SumAndMax;

} catch (java.lang.Throwable e) {

exc=e;

}

}\} {

 $\forall \text{int } i;$ $(0 \leq i \wedge i < \text{a}.\text{length} \wedge \text{inInt}(i)$ $\rightarrow \text{a}[i] \leq \text{self}.\text{max})$ $\wedge (\text{a}.\text{length} > 0$ $\rightarrow \exists \text{int } i;$ $(0 \leq i$ $\wedge i < \text{a}.\text{length}$ $\wedge \text{inInt}(i)$ $\wedge \text{self}.\text{max} = \text{a}[i]))$ $\wedge (\text{self}.\text{sum}$ $= (\text{int})(\text{bsum}(\text{int } i;)(0, \text{a}.\text{length}, \text{a}[i]))$ $\wedge (\text{self}.\text{sum}$ $\leq \text{javaMulInt}(\text{a}.\text{length}, \text{self}.\text{max})$ $\wedge \text{self}.\langle \text{inv} \rangle)$ $\wedge \text{exc} = \text{null}$ $\wedge \forall \text{Field } f;$ $\forall \text{java.lang.Object } o;$ $((o, f) \in \{(\text{self}, \text{SumAndMax}::\text{\$sum}\}$ $\cup \{(\text{self}, \text{SumAndMax}::\text{\$max}\}$ $\vee \neg o = \text{null}$ $\wedge \neg o.\langle \text{created} \rangle @ \text{heapAtPre} = \text{TRUE}$ $\vee o.f = o.f @ \text{heapAtPre})$

Source

SumAndMax.java

```

1 class SumAndMax {
2
3     int sum;
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5
6     /*@ normal_behaviour
7     @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8     @ assignable sum, max;
9     @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10    @ ensures (a.length > 0
11    @         ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12    @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13    @ ensures sum <= a.length * max;
14    @*/
15    void sumAndMax(int[] a) {
16        sum = 0;
17        max = 0;
18        int k = 0;
19
20        /*@ loop_invariant
21        @ 0 <= k && k <= a.length
22        @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23        @ && (k == 0 ==> max == 0)
24        @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25        @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26        @ && sum <= k * max;
27        @
28        @ assignable sum, max;
29        @ decreases a.length - k;
30        @*/
31        while(k < a.length) {
32            if(max < a[k]) {
33                max = a[k];
34            }
35            sum += a[k];
36            k++;
37        }
38    }
39 }
40

```

Show Postcondition/Assignable

File View Proof Options Origin Tracking

Run CVC5, Princess, Z3

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Proofs

-with model src@4:49:20 PM

SumAndMax@SumAndMax::sumAndMax

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0:OPEN GOAL

Current Goal

```

Auto Pilot      Full Auto Pilot      Ctrl+Shift+V
Propositional   Auto Pilot (Preparation Only) Ctrl+Shift+D
Close Provable Goals Below      SMT Preparation      Ctrl+Shift+Y
Flexible Scripting Automation Macro      Finish Symbolic Execution      Ctrl+Shift+X
Simplification  Transcendentals
  A SUMANDMAX::EXACT_LINIS_CORRECT(a,heap) = TRUE
  A (a = null ∨ a.<created> = TRUE)
  A measuredByEmpty
  A ( ∨ int i; (0 ≤ i ∧ i < a.length ∧ inInt(i) → 0 ≤ a[i])
    ∧ (self.<inv> ∧ a = null))
- {heapAtPre:=heap || _a:=a}
  \{
    exc=null;try {
      self.sumAndMax(_a)@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc=e;
    }
  }\> ( ∨ int i;
    ( 0 ≤ i ∧ i < a.length ∧ inInt(i)
      → a[i] ≤ self.max)
  A ( ( a.length > 0
    - ∃ int i;
      ( 0 ≤ i
        ∧ i < a.length
        ∧ inInt(i)
        ∧ self.max = a[i]))
  A ( self.sum
    = (int)(bsum(int i;)(0, a.length, a[i]))
  A ( self.sum
    ≤ javaMulInt(a.length, self.max)
    ∧ self.<inv>))
  A exc = null
  A ∨ Field f;
  ∨ java.lang.Object o;
  ( (o, f) ∈ {(self, SumAndMax::$sum)
    U {(self, SumAndMax::$max)}}
  ∨ o = null
  ∧ o.<created>@heapAtPre = TRUE
  ∨ o.f = o.f@heapAtPre)

```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7     @ requires (forall int i; 0 <= i && i < a.length; 0 <= a[i]);
8     @ assignable sum, max;
9     @ ensures (forall int i; 0 <= i && i < a.length; a[i] <= max);
10    @ ensures (a.length > 0
11      @ ==> (exists int i; 0 <= i && i < a.length; max == a[i]));
12    @ ensures sum == (sum int i; 0 <= i && i < a.length; a[i]);
13    @ ensures sum <= a.length * max;
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15   void sumAndMax(int[] a) {
16     sum = 0;
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20     /*@ loop_invariant
21       @ 0 <= k && k <= a.length
22       @ && (forall int i; 0 <= i && i < k; a[i] <= max)
23       @ && (k == 0 ==> max == 0)
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25       @ && sum == (sum int i; 0 <= i && i < k; a[i])
26       @ && sum <= k * max;
27       @
28       @ assignable a.length, max;
29       @ decreases a.length - k;
30       @*/
31   while(k < a.length) {
32     if(max < a[k]) {
33       max = a[k];
34     }
35     sum += a[k];
36     k++;
37   }
38 }
39 }
40

```

Show Postcondition/Assignable

KeY Proof has been pruned: one open goal remains.

Show log

KeY 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

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SumAndMax(SumAndMax:SumAndMax)

Proof Search Strategy Goals

Proof Info

Proof

Null Reference

523:Closed goal

Index Out of Bounds

521:Closed goal

Null Reference

449:Closed goal

Null Reference

447:Closed goal

Index Out of Bounds

445:Closed goal

If x_5 false

Normal Execution

Normal Execution

CUT: k_0

CUT: k_0

Null Reference

2169:Closed goal

Null Reference

2171:Closed goal

Index Out of Bounds

2240:Closed goal

Null Reference

2242:Closed goal

Null Reference (a = null)

2333:Closed goal

Index Out of Bounds

2397:Closed goal

If x_2 false

361:OPEN GOAL

Null Reference (a = null)

2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0)]]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
  ∀ int i;
    ( i ≥ 0 ∧ i < a.length
    → a[i]@heap[self.sum := 0]
      [self.max := 0]
      [anon( {(self, SumAndMax::$max)}
          U {(self, SumAndMax::$sum)},
          anon_heap_LOOP_0)]]
    ≤ self.max@heap[self.sum := 0]
      [self.max := 0]
      [anon( {(self, SumAndMax::$max)}
          U {(self, SumAndMax::$sum)},
          anon_heap_LOOP_0)]]
  ∧ ( ( a.length > 0
    → ∃ int i;
      ( i ≥ 0
      ∧ i < a.length
      ∧ a[i]@heap[self.sum := 0]
        [self.max := 0]
        [anon( {(self, SumAndMax::$max)}
            U {(self, SumAndMax::$sum)},
            anon_heap_LOOP_0)]]
    )
  )

```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    * requires (∀forall int i; 0 ≤ i && i < a.length; 0 ≤ a[i]);
8    * @ assignable sum, max;
9    * @ ensures (∀forall int i; 0 ≤ i && i < a.length; a[i] ≤ max);
10   * @ ensures (a.length > 0
11   *           ==> (∀exists int i; 0 ≤ i && i < a.length; max == a[i]));
12   * @ ensures sum == (∑sum int i; 0 ≤ i && i < a.length; a[i]);
13   * @ ensures sum ≤ a.length * max;
14   */
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21     * 0 ≤ k && k ≤ a.length
22     * && (∀forall int i; 0 ≤ i && i < k; a[i] ≤ max)
23     * && (k == 0 ==> max == 0)
24     * && (k > 0 ==> (∀exists int i; 0 ≤ i && i < k; max == a[i]))
25     * && sum == (∑sum int i; 0 ≤ i && i < k; a[i])
26     * && sum ≤ k * max;
27     *
28     * @ assignable sum, max;
29     * @ decreases a.length - k;
30     */
31     while(k < a.length)
32       if(max < a[k]) {
33         max = a[k];
34       }
35     sum += a[k];
36     k++;
37   }
38 }
39
40

```

Normal Execution (a != null)

Show log

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File View Proof Options Origin Tracking

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Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

with model src@8:15:22 PM

SumAndMax(SumAndMax:SumAndMax)

Proof Search Strategy Goals

Proof Info

Proof

Null Referenc... 523:Clo...
 Index Out... 521:Clo...
 Null Referen... 449:Close...
 Null Reference... 447:Closed g...
 Index Out of B... 445:Closed g...
 If x_5 false
 Normal Executi...
 Normal Exec...
 Normal Ex...
 CUT: k...
 CUT: k...
 Null Referen... 2169:Cl...
 Null Reference... 2171:Close...
 Index Out of... 2240:Close...
 Null Reference... 2242:Closed...
 Null Reference (a =... 2333:Closed goal
 Index Out of Bounds... 2397:Closed goal
 If x_2 false
 361:OPEN GOAL
 Null Reference (a = null) 2244:Closed goal
 how Axiom Satisfiability

Sequent

```

bsum(int i;){0,
  k_0,
  a[i]@heap[self.sum := 0]
  [self.max := 0]
  [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0))]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
→
k_0 < a.length,
self = null,
a = null,
  ∀ int i;
    ( i ≥ 0 ∧ i < a.length
    → a[i]@heap[self.sum := 0]
      [self.max := 0]
      [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0))]
    ≤ self.max@heap[self.sum := 0]
      [self.max := 0]
      [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0))]
  ∧ ( ( a.length > 0
    → ∃ int i;
      ( i ≥ 0
        ∧ i < a.length
        ∧ a[i]@heap[self.sum := 0]
          [self.max := 0]
          [anon( {(self, SumAndMax::$max)}
            U {(self, SumAndMax::$sum)},
            anon_heap_LOOP_0))]
      )
    )
  )

```

Source

```

SumAndMax.java
1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7     @ requires (forall int i; 0 <= i && i < a.length; 0 <= a[i]);
8     @ assignable sum, max;
9     @ ensures (forall int i; 0 <= i && i < a.length; a[i] <= max);
10    @ ensures (a.length > 0
11    @     ==> (forall int i; 0 <= i && i < a.length; max == a[i]));
12    @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13    @ ensures sum <= a.length * max;
14    */
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int i;
19
20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ && (forall int i; 0 <= i && i < k; a[i] <= max)
23     @ && (k == 0 ==> max == 0)
24     @ && (k > 0 ==> (forall int i; 0 <= i && i < k; max == a[i]))
25     @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @
28     @ assignable sum, max;
29     @ decreases a.length - k;
30     */
31     while(k < a.length)
32       if(max < a[k]) {
33         max = a[k];
34       }
35     sum += a[k];
36     k++;
37   }
38 }
39
40

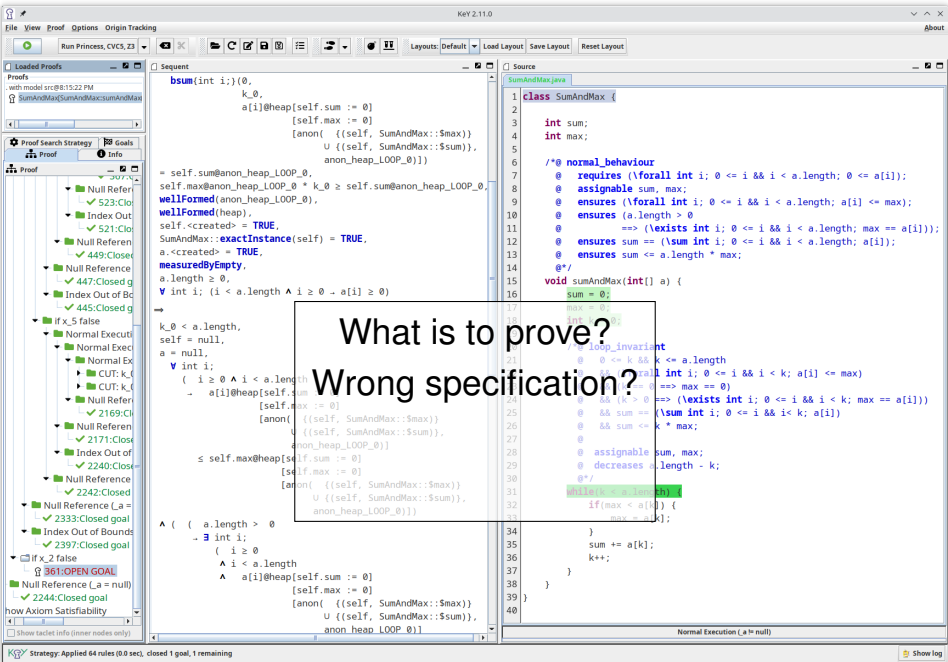
```

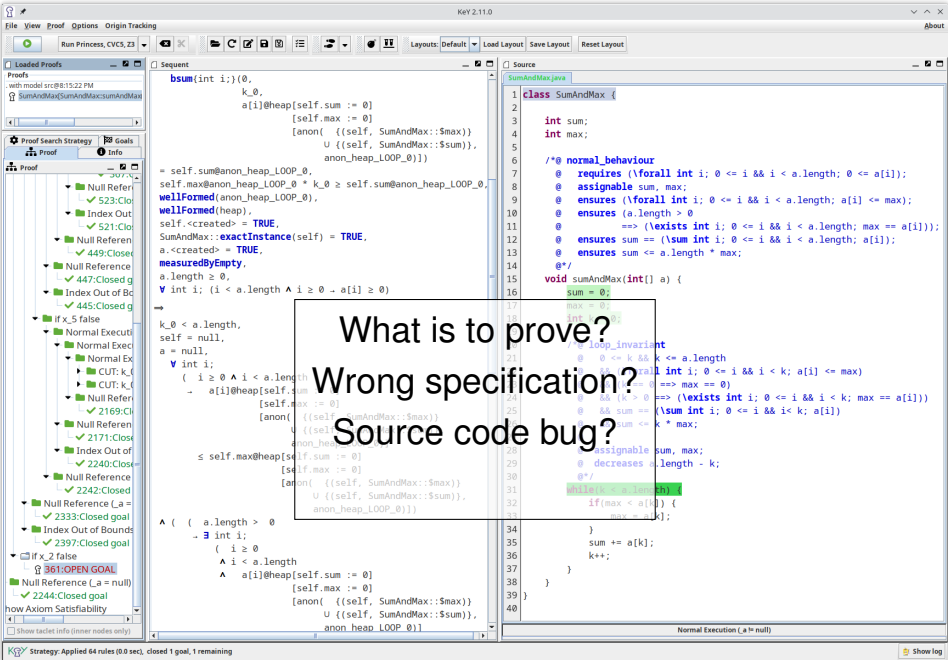
Normal Execution (a != null)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Show log

What is to prove?





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Proofs

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SumAndMax(SumAndMax:sumAndMax)

Proof Search Strategy

Goals

Proof

Info

Null Reference

Index Out of Bounds

Null Reference

Index Out of Bounds

If x_5 false

Normal Execution

CUT: k_0

CUT: k_1

Null Reference

Null Reference

Index Out of Bounds

Null Reference

Null Reference (a = null)

Index Out of Bounds

If x_2 false

Null Reference (a = null)

how Axiom Satisfiability

Show tactic info (inner nodes only)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Sequent

```
bsum(int i;){0,
  k_0,
  a[i]@heap[self.sum := 0]
  [self.max := 0]
  [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
→
k_0 < a.length,
self = null,
a = null,
∀ int i;
( i ≥ 0 ∧ i < a.length
→ a[i]@heap[self.sum := 0]
  [self.max := 0]
  [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]]
≤ self.max@heap[self.sum := 0]
  [self.max := 0]
  [anon( {(self, SumAndMax::$sum)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]]
∧ ( ( a.length > 0
→ ∃ int i;
( i ≥ 0
∧ i < a.length
∧ a[i]@heap[self.sum := 0]
  [self.max := 0]
  [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0) ) )
```

Source

```
SumAndMax.java
1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (forall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (forall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @ ==> (forall int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int i;
19
20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ 0 <= i && i < k; a[i] <= max
23     @ k >= 0 ==> max == 0
24     @ (forall int i; 0 <= i && i < k; max == a[i])
25     @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @ assignable sum, max;
28     @ decreases a.length - k;
29     @ invariant (a.length > 0
30     @ if (max < a[k]) {
31     @   max = a[k];
32     @ }
33     @ )
34   }
35   sum += a[k];
36   k++;
37 }
38 }
39 }
40 }
```

Normal Execution (a != null)

Show log

What is to prove?
Wrong specification?
Source code bug?
Prover needs help?

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Proofs

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SumAndMax(SumAndMax:SumAndMax)

Proof Search Strategy Goals

Proof Info

Proof

Null Refer ✓ 523:Clo

Index Out ✓ 521:Clo

Null Referen ✓ 449:Close

Null Reference ✓ 447:Closed g

Index Out of Bc ✓ 445:Closed g

If x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_0

CUT: k_0

Null Refer ✓ 2169:Cl

Null Referen ✓ 2171:Close

Index Out of ✓ 2240:Close

Null Reference ✓ 2242:Closed

Null Reference (a = ✓ 2333:Closed goal

Index Out of Bounds ✓ 2397:Closed goal

If x_2 false

361:OPEN GOAL

Null Reference (a = null) ✓ 2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0)]]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
  ∀ int i;
    ( i ≥ 0 ∧ i < a.length
    → a[i]@heap[self.sum := 0]
      [self.max := 0]
      [anon( {(self, SumAndMax::$max)}
          U {(self, SumAndMax::$sum)},
          anon_heap_LOOP_0)]
      ≤ self.max@heap[self.sum := 0]
        [self.max := 0]
        [anon( {(self, SumAndMax::$max)}
            U {(self, SumAndMax::$sum)},
            anon_heap_LOOP_0)])
A ( ( a.length > 0
    → ∃ int i;
      ( i ≥ 0
      ∧ i < a.length
      ∧ a[i]@heap[self.sum := 0]
        [self.max := 0]
        [anon( {(self, SumAndMax::$max)}
            U {(self, SumAndMax::$sum)},
            anon_heap_LOOP_0)]

```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    * requires (∀forall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    * @ assignable sum, max;
9    * @ ensures (∀forall int i; 0 <= i && i < a.length; a[i] <= max);
10   * @ ensures (a.length > 0
11   *           ==> (∀exists int i; 0 <= i && i < a.length; max == a[i]));
12   * @ ensures sum == (∑sum int i; 0 <= i && i < a.length; a[i]);
13   * @ ensures sum <= a.length * max;
14   */
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21     * 0 <= k && k <= a.length
22     * && (∀forall int i; 0 <= i && i < k; a[i] <= max)
23     * && (k == 0 ==> max == 0)
24     * && (k > 0 ==> (∀exists int i; 0 <= i && i < k; max == a[i]))
25     * && sum == (∑sum int i; 0 <= i && i < k; a[i])
26     * && sum <= k * max;
27     *
28     * @ assignable sum, max;
29     * @ decreases a.length - k;
30     */
31     while(k < a.length)
32       if(max < a[k]) {
33         max = a[k];
34       }
35     sum += a[k];
36     k++;
37   }
38 }
39
40

```

Normal Execution (a != null)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Show log

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SumAndMax(SumAndMax:SumAndMax)

Proof Search Strategy Goals

Proof Info

Proof

Null Refer ✓ 523:Clo

Index Out ✓ 521:Clo

Null Referen ✓ 449:Close

Null Reference ✓ 447:Closed g

Index Out of Bc ✓ 445:Closed g

If x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_0

CUT: k_0

Null Refer ✓ 2169:Cl

Null Referen ✓ 2171:Close

Index Out of ✓ 2240:Close

Null Reference ✓ 2242:Closed

Null Reference (a = ✓ 2333:Closed goal

Index Out of Bounds ✓ 2397:Closed goal

If x_2 false

361:OPEN GOAL

Null Reference (a = null) ✓ 2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0))]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
∀ int i;
( i ≥ 0 ∧ i < a.length
  → a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0))]
  ≤ self.max@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0))]
∧ ( ( a.length > 0
  → ∃ int i;
    ( i ≥ 0
      ∧ i < a.length
        ∧ a[i]@heap[self.sum := 0]
          [self.max := 0]
          [anon( {(self, SumAndMax::$max)}
              U {(self, SumAndMax::$sum)},
              anon_heap_LOOP_0)]
    )
  )
  )

```

valid Java heap

Source

SumAndMax.java

```

1 class SumAndMax {
2
3 int sum;
4 int max;
5
6 /*@ normal_behaviour
7 @ requires (∀forall int i; 0 <= i && i < a.length; 0 <= a[i]);
8 @ assignable sum, max;
9 @ ensures (∀forall int i; 0 <= i && i < a.length; a[i] <= max);
10 @ ensures (a.length > 0
11 @ ==> (∀exists int i; 0 <= i && i < a.length; max == a[i]));
12 @ ensures sum == (∑sum int i; 0 <= i && i < a.length; a[i]);
13 @ ensures sum <= a.length * max;
14 */
15 void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20 /*@ loop_invariant
21 @ 0 <= k && k <= a.length
22 @ && (∀forall int i; 0 <= i && i < k; a[i] <= max)
23 @ && (k == 0 ==> max == 0)
24 @ && (k > 0 ==> (∀exists int i; 0 <= i && i < k; max == a[i]))
25 @ && sum == (∑sum int i; 0 <= i && i < k; a[i])
26 @ && sum <= k * max;
27 @
28 @ assignable sum, max;
29 @ decreases a.length - k;
30 */
31 while(k < a.length)
32     if(max < a[k]) {
33         max = a[k];
34     }
35     sum += a[k];
36     k++;
37 }
38
39 }
40

```

Normal Execution (a != null)

Show log

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Proofs

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SumAndMax(SumAndMax:SumAndMax)

Proof Search Strategy Goals

Proof Info

Proof

Null Refer ✓ 523:Clo

Index Out ✓ 521:Clo

Null Refer ✓ 449:Close

Null Reference ✓ 447:Closed g

Index Out of Bc ✓ 445:Closed g

If x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_0

CUT: k_0

Null Refer ✓ 2169:Cl

Null Referen ✓ 2171:Close

Index Out of ✓ 2240:Close

Null Reference ✓ 2242:Closed

Null Reference (a = ✓ 2333:Closed goal

Index Out of Bounds ✓ 2397:Closed goal

If x_2 false

361:OPEN GOAL

Null Reference (a = null) ✓ 2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0))]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
→
k_0 < a.length,
self = null,
a = null,
∀ int i;
( i ≥ 0 ∧ i < a.length
→ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]
≤ self.max@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0))]
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( i ≥ 0
∧ i < a.length
∧ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]

```

valid Java heap
type information

Source

```

SumAndMax.java
1 class SumAndMax {
2
3 int sum;
4 int max;
5
6 /*@ normal_behaviour
7 @ requires (∀forall int i; 0 <= i && i < a.length; 0 <= a[i]);
8 @ assignable sum, max;
9 @ ensures (∀forall int i; 0 <= i && i < a.length; a[i] <= max);
10 @ ensures (a.length > 0
11 @ ==> (∀exists int i; 0 <= i && i < a.length; max == a[i]));
12 @ ensures sum == (∑sum int i; 0 <= i && i < a.length; a[i]);
13 @ ensures sum <= a.length * max;
14 */
15 void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20 /*@ loop_invariant
21 @ 0 <= k && k <= a.length
22 @ && (∀forall int i; 0 <= i && i < k; a[i] <= max)
23 @ && (k == 0 ==> max == 0)
24 @ && (k > 0 ==> (∀exists int i; 0 <= i && i < k; max == a[i]))
25 @ && sum == (∑sum int i; 0 <= i && i < k; a[i])
26 @ && sum <= k * max;
27 @
28 @ assignable sum, max;
29 @ decreases a.length - k;
30 */
31 while(k < a.length)
32     if(max < a[k]) {
33         max = a[k];
34     }
35     sum += a[k];
36     k++;
37 }
38 }
39 }
40

```

Normal Execution (a != null)

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Loaded Proofs

Proofs

with model src@8:15:22 PM

SumAndMax(SumAndMax:SumAndMax)

Proof Search Strategy Goals

Proof Info

Proof

Null Refer ✓ 523:Clo

Index Out ✓ 521:Clo

Null Refer ✓ 449:Close

Null Reference ✓ 447:Closed g

Index Out of Bc ✓ 445:Closed g

If x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_0

CUT: k_0

Null Refer ✓ 2169:Cl

Null Refer ✓ 2171:Close

Index Out of ✓ 2240:Close

Null Reference ✓ 2242:Closed

Null Reference (a = ✓ 2333:Closed goal

Index Out of Bounds ✓ 2397:Closed goal

If x_2 false

361:OPEN GOAL

Null Reference (a = null) ✓ 2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0))]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
v int i; (i < a.length ^ i ≥ 0 -> a[i] ≥ 0)
→
k_0 < a.length,
self = null,
a = null,
v int i;
( i ≥ 0 ^ i < a.length
- a[i]@heap[self.sum := 0]
  [self.max := 0]
  [anon( {(self, SumAndMax::$max)}
      U {(self, SumAndMax::$sum)},
      anon_heap_LOOP_0))]
≤ self.max@heap[self.sum := 0]
  [self.max := 0]
  [anon( {(self, SumAndMax::$max)}
      U {(self, SumAndMax::$sum)},
      anon_heap_LOOP_0))]
A ( ( a.length > 0
- v int i;
  ( i ≥ 0
    ^ i < a.length
    ^ a[i]@heap[self.sum := 0]
      [self.max := 0]
      [anon( {(self, SumAndMax::$max)}
          U {(self, SumAndMax::$sum)},
          anon_heap_LOOP_0)]
  )
)

```

valid Java heap
type information
no termination witness

Source

SumAndMax.java

```

1 class SumAndMax {
2
3 int sum;
4 int max;
5
6 /*@ normal_behaviour
7 @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8 @ assignable sum, max;
9 @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10 @ ensures (a.length > 0
11 @ ==> (\existsists int i; 0 <= i && i < a.length; max == a[i]));
12 @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13 @ ensures sum <= a.length * max;
14 */
15 void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20 /*@ loop_invariant
21 @ 0 <= k && k <= a.length
22 @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23 @ && (k == 0 ==> max == 0)
24 @ && (k > 0 ==> (\existsists int i; 0 <= i && i < k; max == a[i]))
25 @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26 @ && sum <= k * max;
27 @
28 @ assignable sum, max;
29 @ decreases a.length - k;
30 */
31 while(k < a.length)
32     if(max < a[k]) {
33         max = a[k];
34     }
35     sum += a[k];
36     k++;
37 }
38
39 }
40

```

Normal Execution (a != null)

Show log

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

 Proofs
 .with model src@8:15:22 PM
 SumAndMax(SumAndMax:SumAndMax)

Proof Search Strategy

Goals

Proof

Info

Proof

Null Refer

Index Out

Null Referen

Index Out of Bc

Null Reference

Index Out of Bc

If x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_0

CUT: k_0

Null Refer

Null Referen

Index Out of

Null Reference

Index Out of Bc

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k_0 < a.length,
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    ≤ self.max@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)])
  ∧ ( ( a.length > 0
    → ∃ int i;
      ( i ≥ 0
      ∧ i < a.length
      ∧ a[i]@heap[self.sum := 0]
      [self.max := 0]
      [anon( {(self, SumAndMax::$max)}
      U {(self, SumAndMax::$sum)},
      anon_heap_LOOP_0)]
      )
    )
  )

```

heap encoding

Source

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6   /*@ normal_behaviour
7    @ requires (∀forall int i; 0 <= i && i < a.length; 0 <= a[i]);
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10   @ ensures (a.length > 0
11   @ ==> (∀exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (∑sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   */
15   void sumAndMax(int[] a) {
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20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ && (∀forall int i; 0 <= i && i < k; a[i] <= max)
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24     @ && (k > 0 ==> (∀exists int i; 0 <= i && i < k; max == a[i]))
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26     @ && sum <= k * max;
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28     @ assignable sum, max;
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35     sum += a[k];
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```

Normal Execution (a != null)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Show log

Summary

Idea

Combined view for source, specification, and proof state

- that facilitates understanding of the current proof situation,
- which the user can interact with,
- with which (hopefully) most Java programs can be verified.

Open Questions

- How can formulas be represented that relate multiple heap states?
- How can framing clauses be represented?
- What about multiple modalities (queries, information flow, ...)?